

Galaxy Clustering

PH 7th June 2021

N-Point Statistics

Number counts/histogram
luminosity/analyses

~ Mean

~ $\langle N \rangle$

1-point statistics

1

Galaxy clustering/
powerspectrum/
2-point correlation
function

~ Standard Deviation

~ $\langle N^2 \rangle$

2-point statistics

2

Bispectrum/
3-point correlation
function

~ Skew

~ $\langle N^3 \rangle$

3-point statistics

3

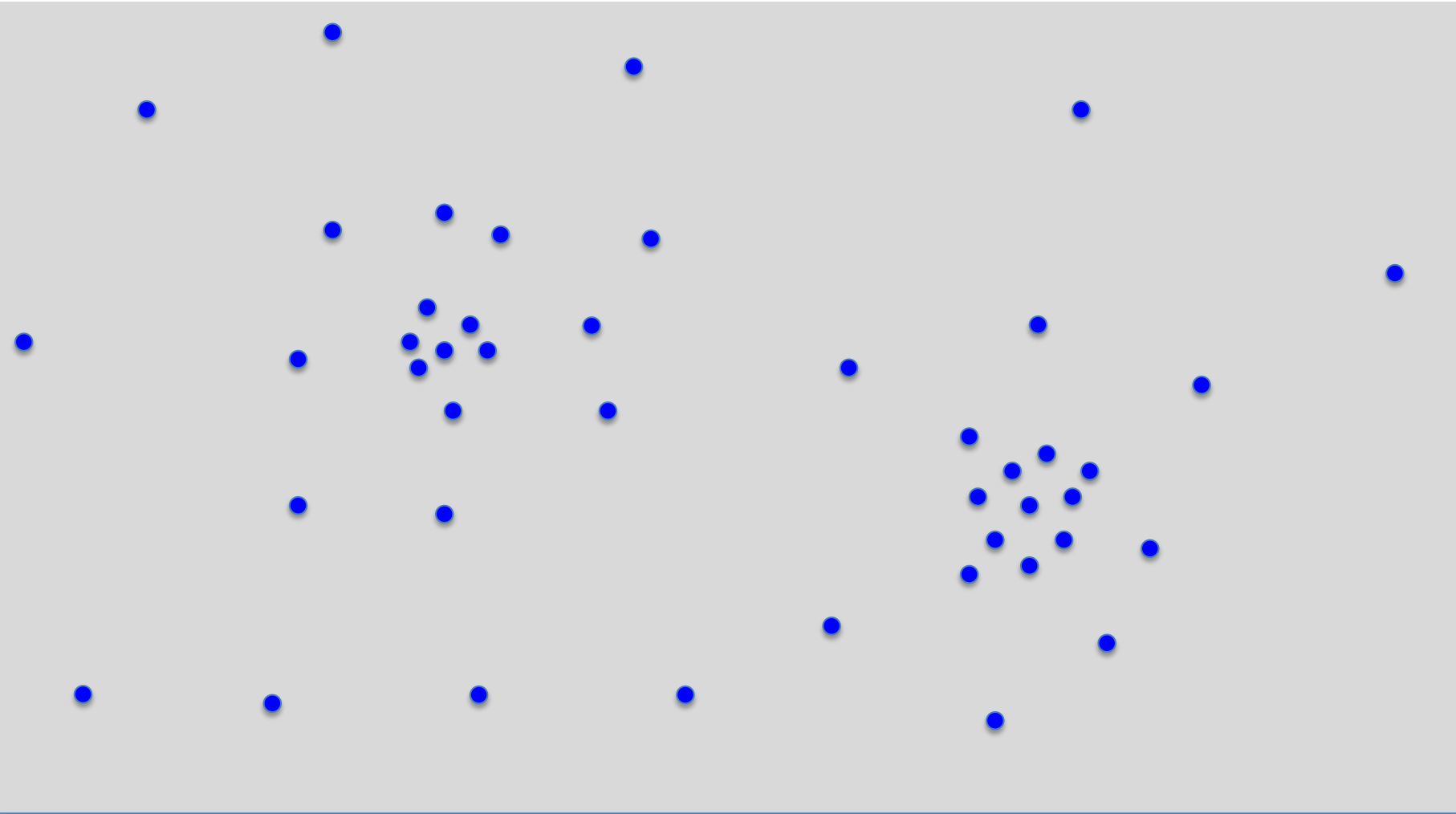
Trispectrum/
4-point correlation
function

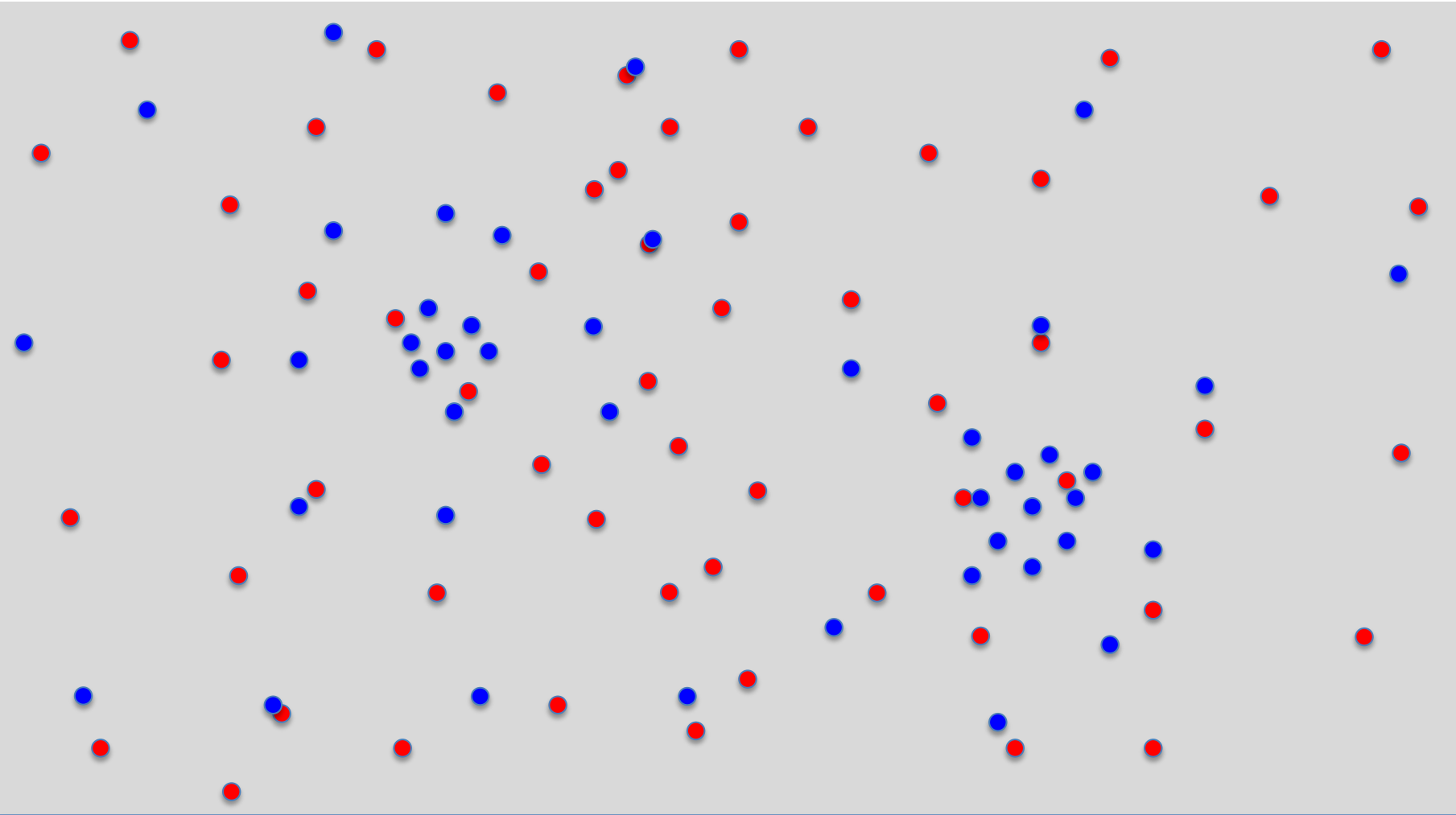
~ kurtosis

~ $\langle N^4 \rangle$

4-point statistics

4

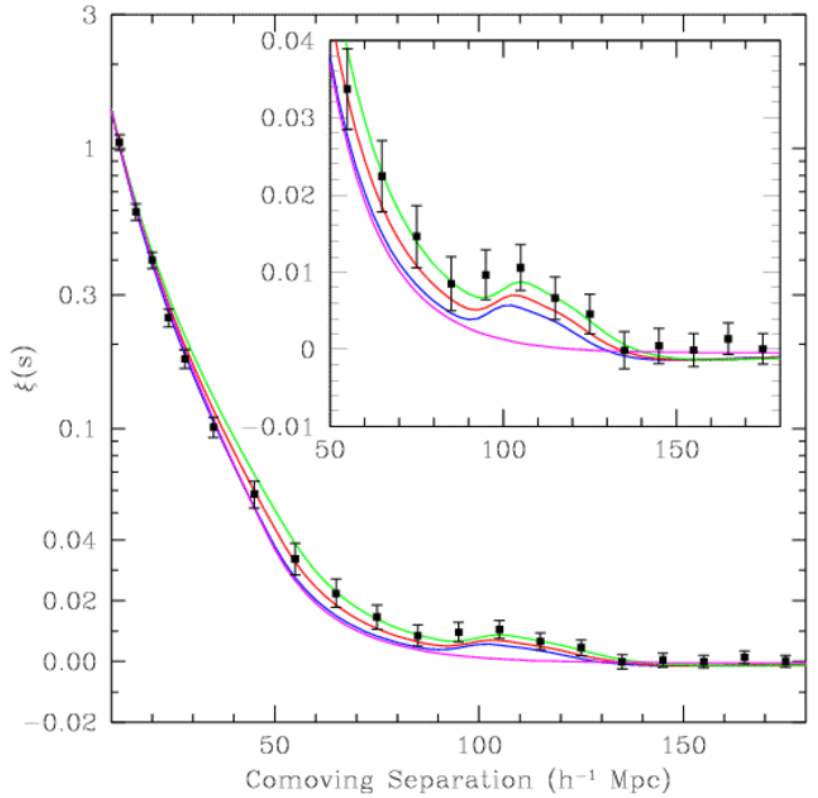
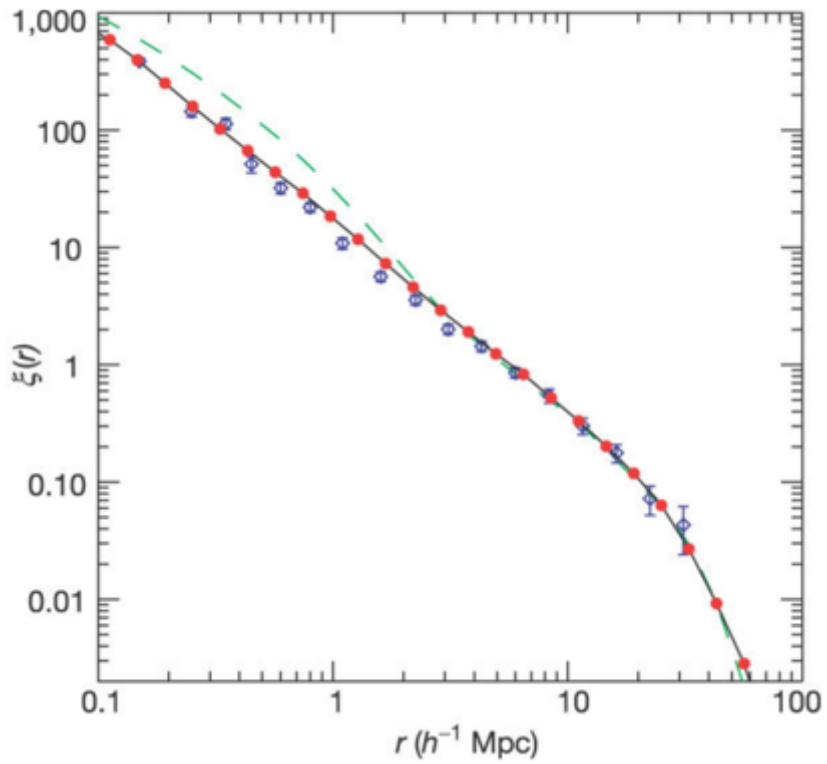




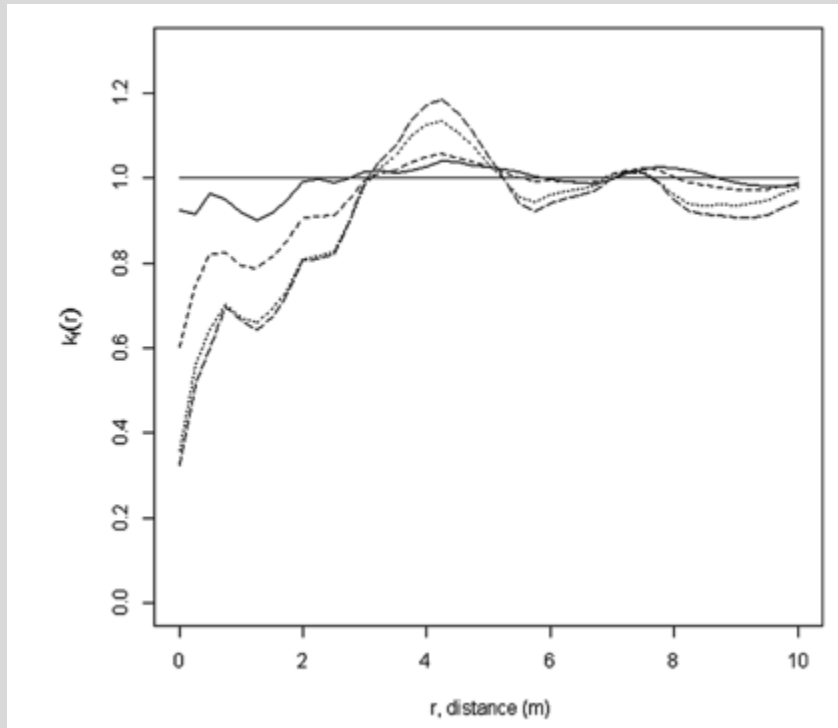
$$\omega(\theta) = \frac{DD}{RR} - 1$$

$$\omega(\theta) = \frac{DD - 2DR + RR}{RR},$$

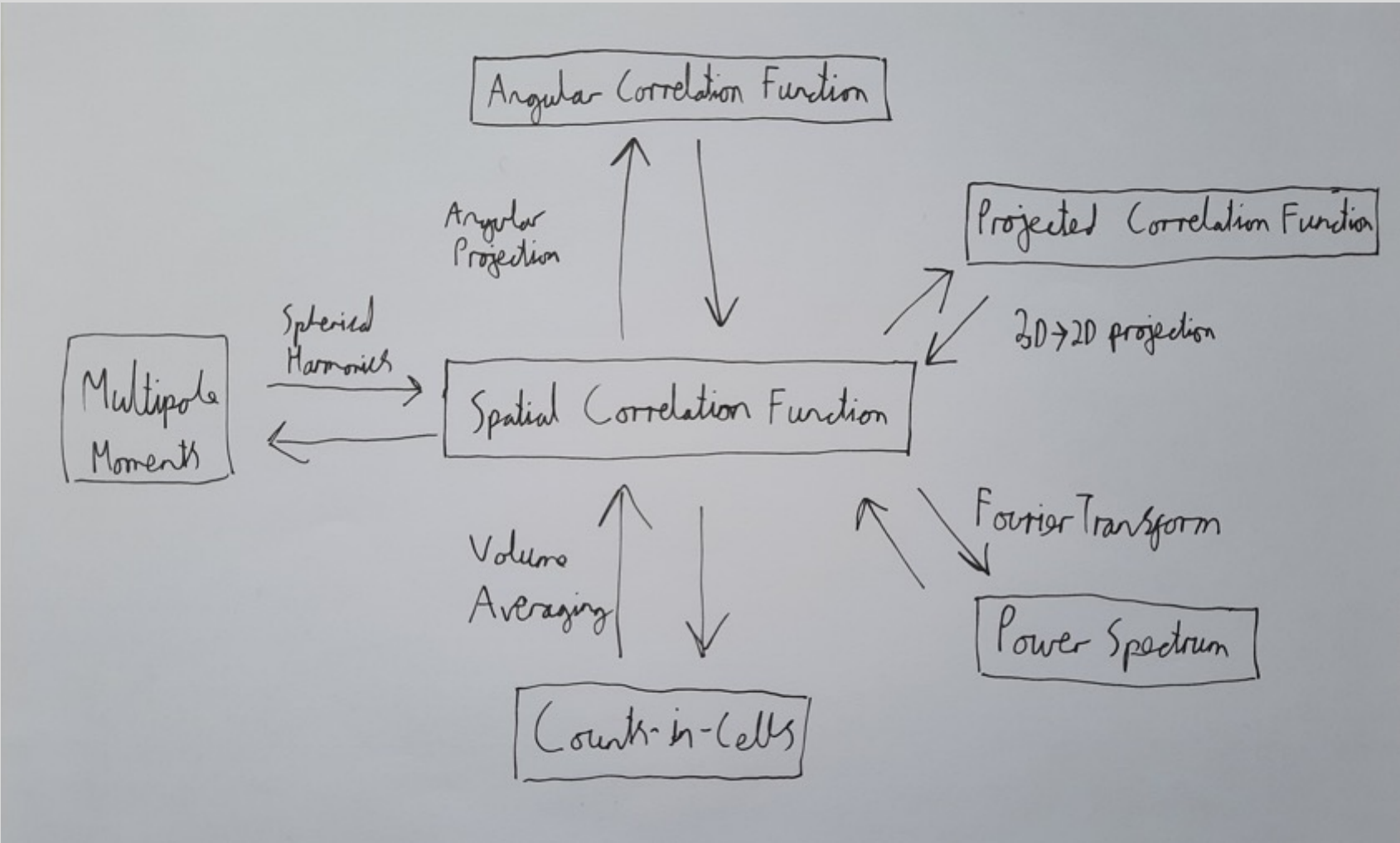
Example Measurements



Example Measurements



Different Representations

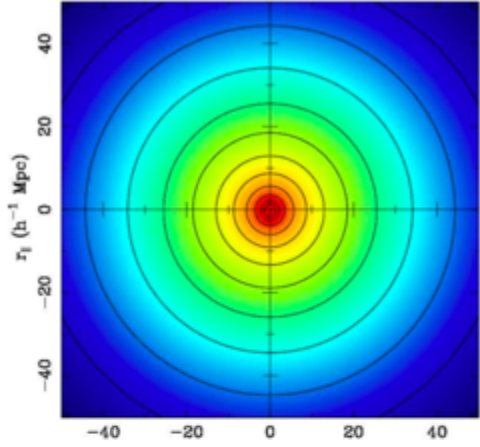


- **Auto**-Correlation Function: Clustering of a single sample
- **Cross**-Correlation Function: Clustering between two samples

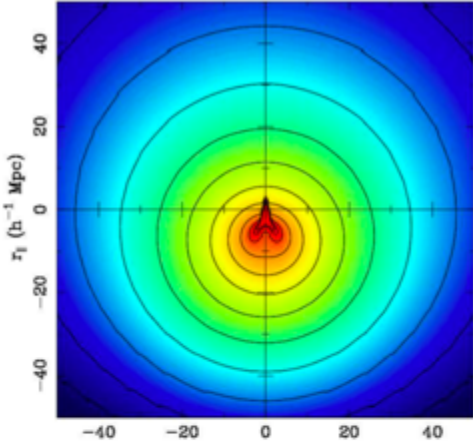
- Galaxy Clustering: Gives galaxy auto-correlation
- Galaxy-Galaxy Lensing: Gives galaxy-DM cross-correlation
- Weak Lensing: Gives total matter auto-correlation

Also used for HI reionisation signal, CMB and more...

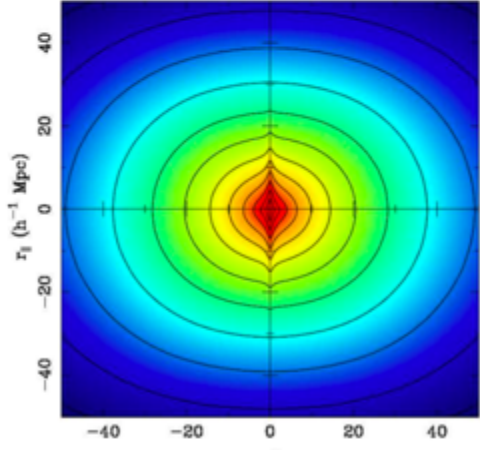
3D Effects



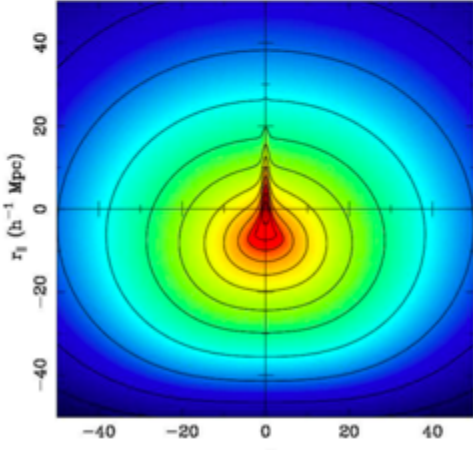
(a) Real space



(b) With grav. redshifts $\times 500$

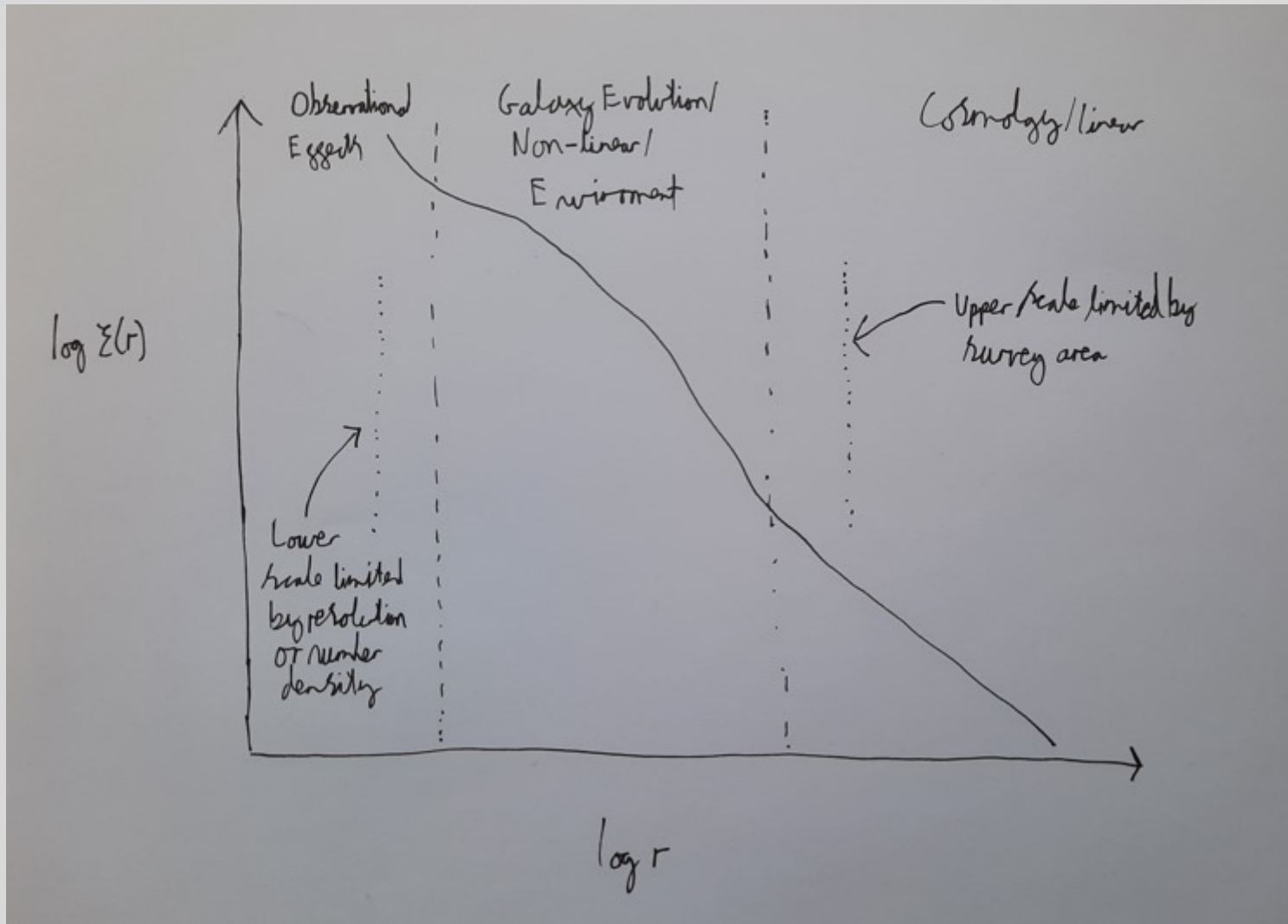


(c) With pec. vels.



(d) With grav. redshifts $\times 500$ and pec. vels.

Scales



Observational Effects

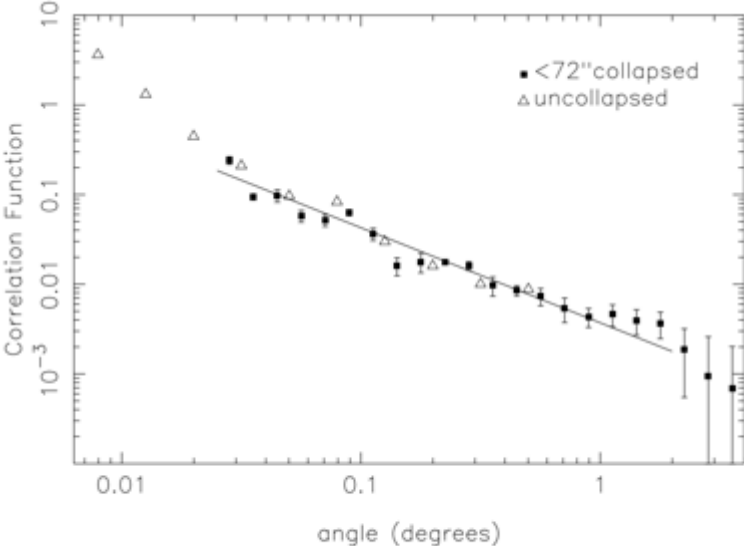
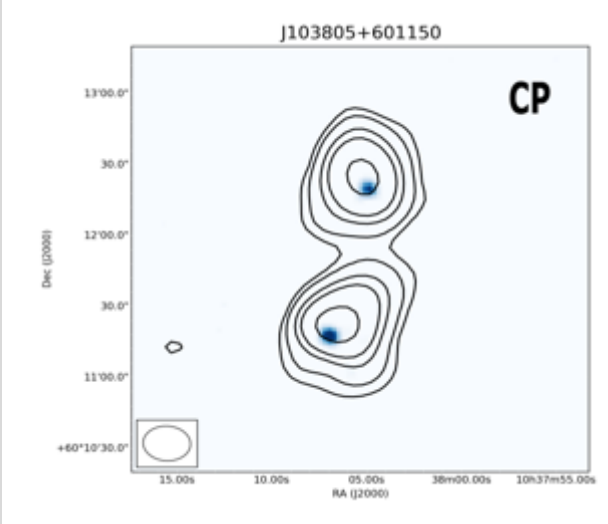
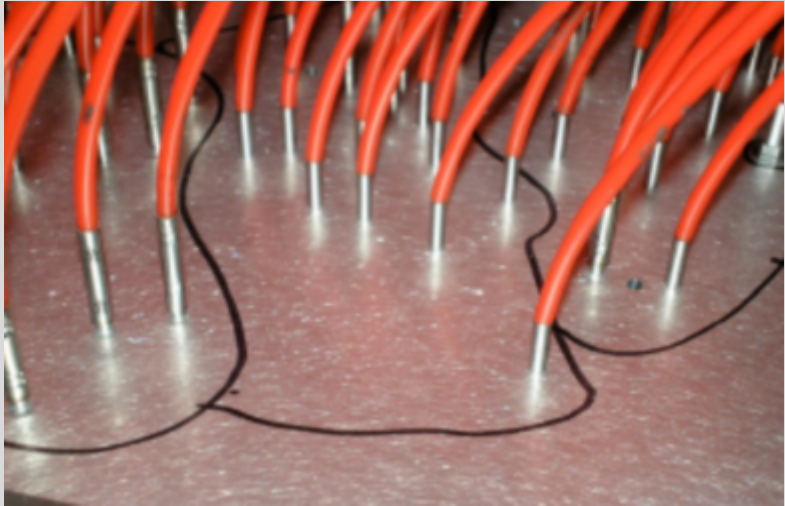
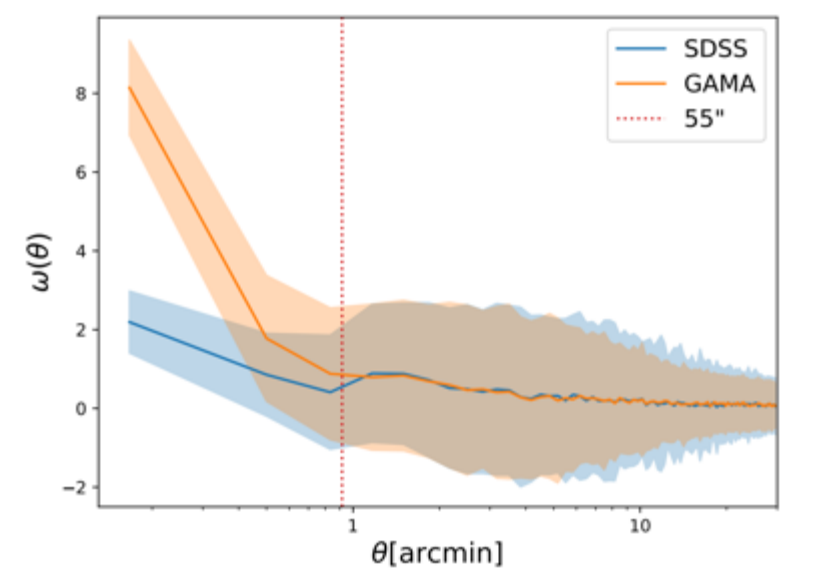


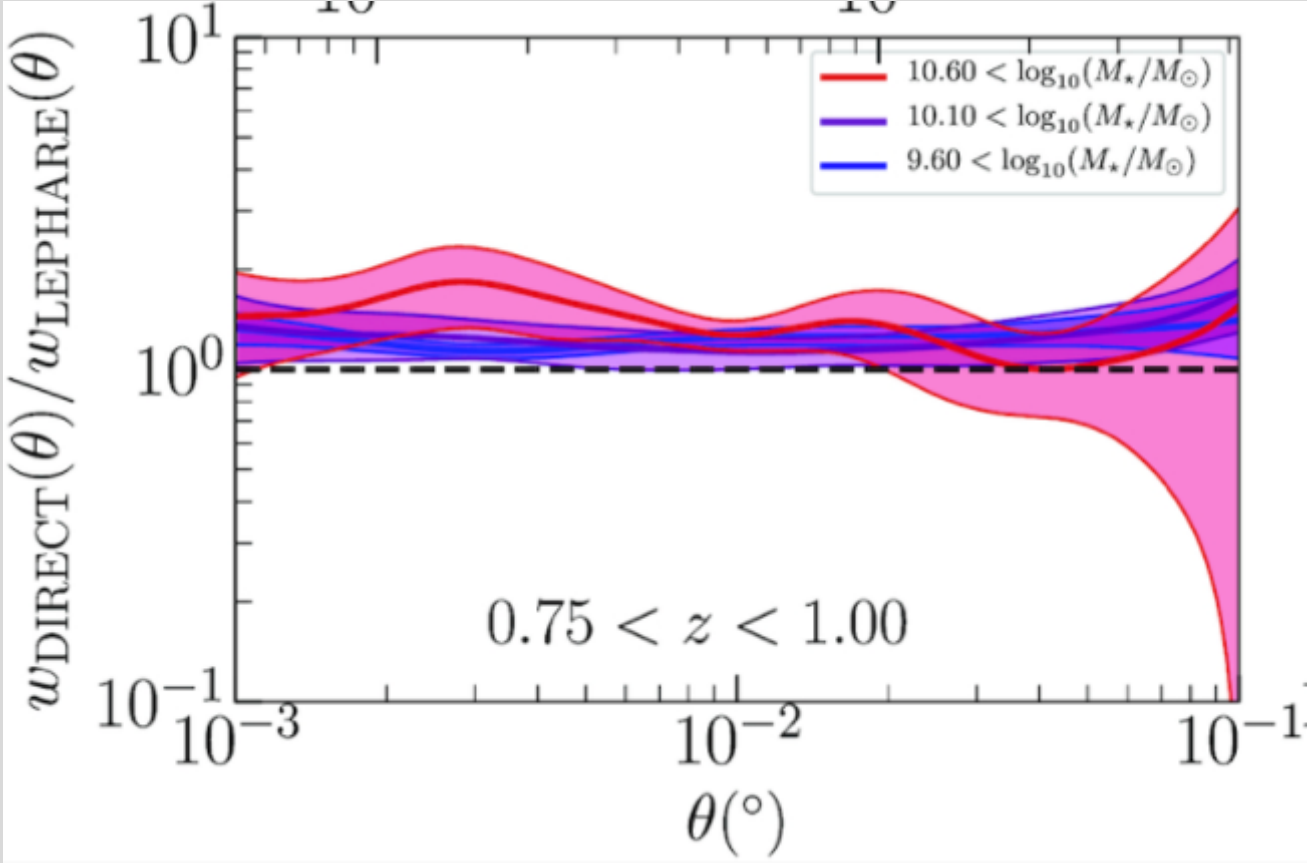
FIG. 1.—The filled squares show the autocorrelation function [$w(\theta) = 2DD/DR - 1$] calculated for the whole sample (109,873 sources, where sources separated by less than 0".02 have been collapsed to a single source). The open triangles show the correlation function obtained when sources are not collapsed. Error bars are obtained using the bootstrapping technique described in § 3.



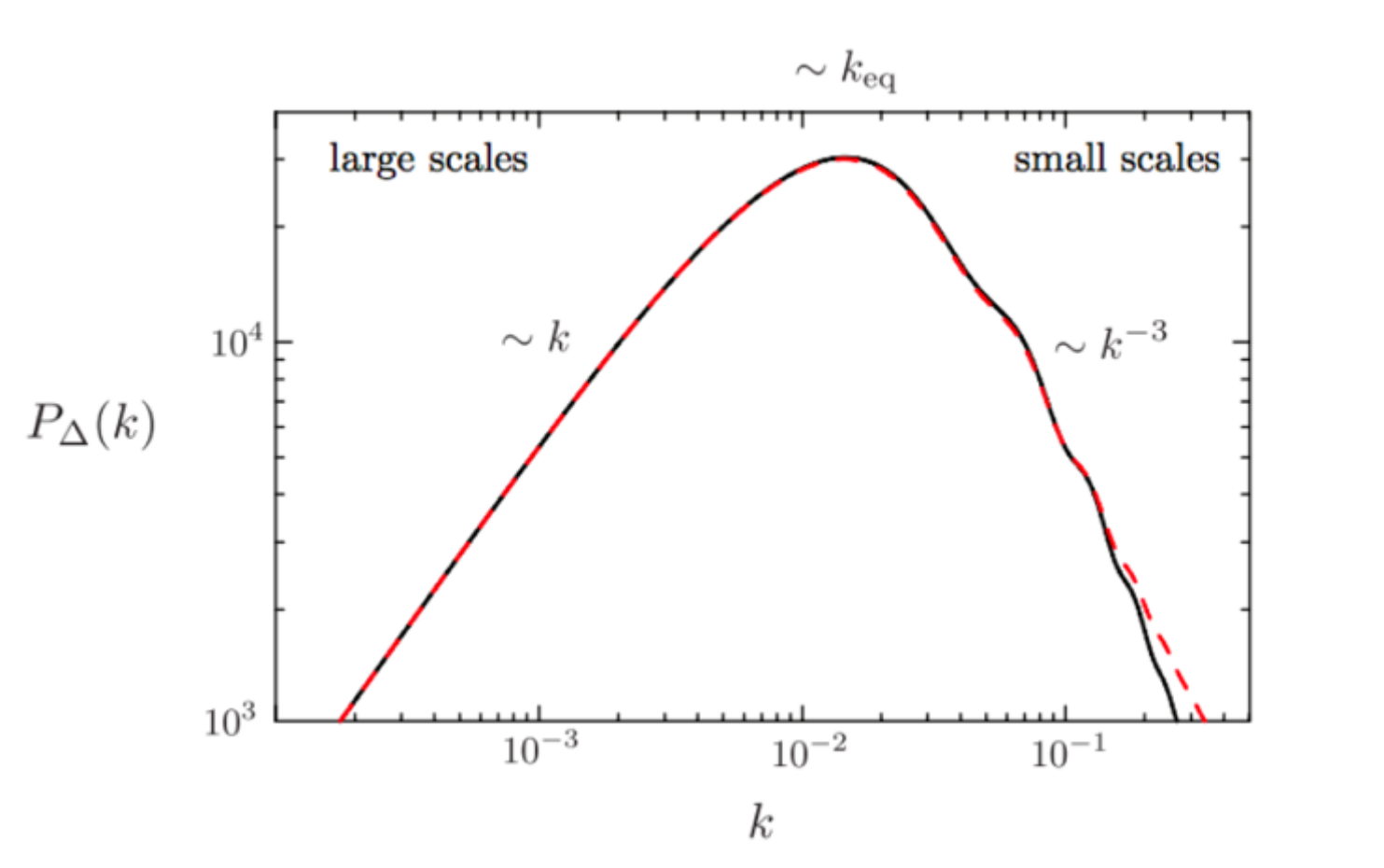
Observational Effects



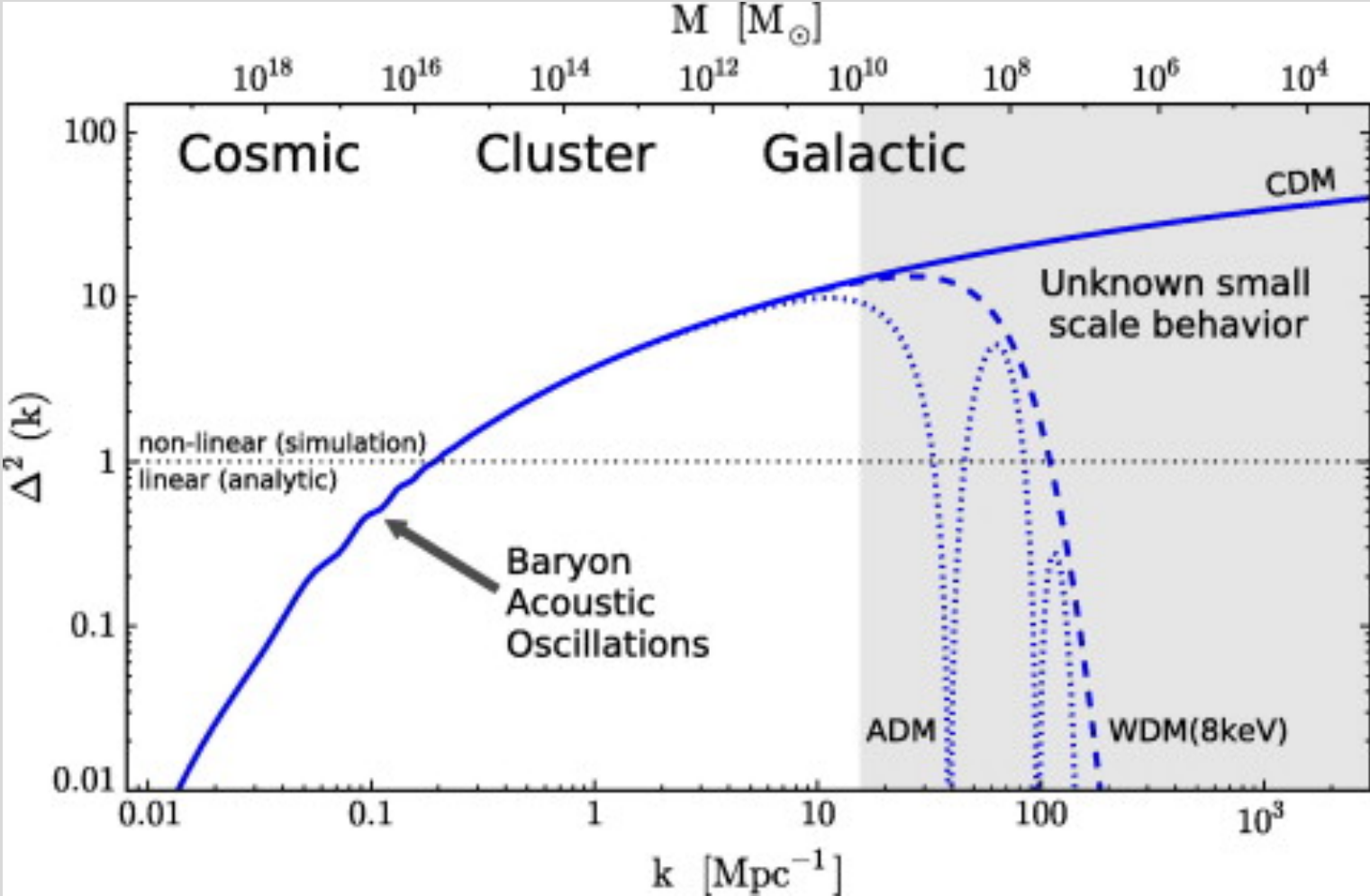
Observational Effects



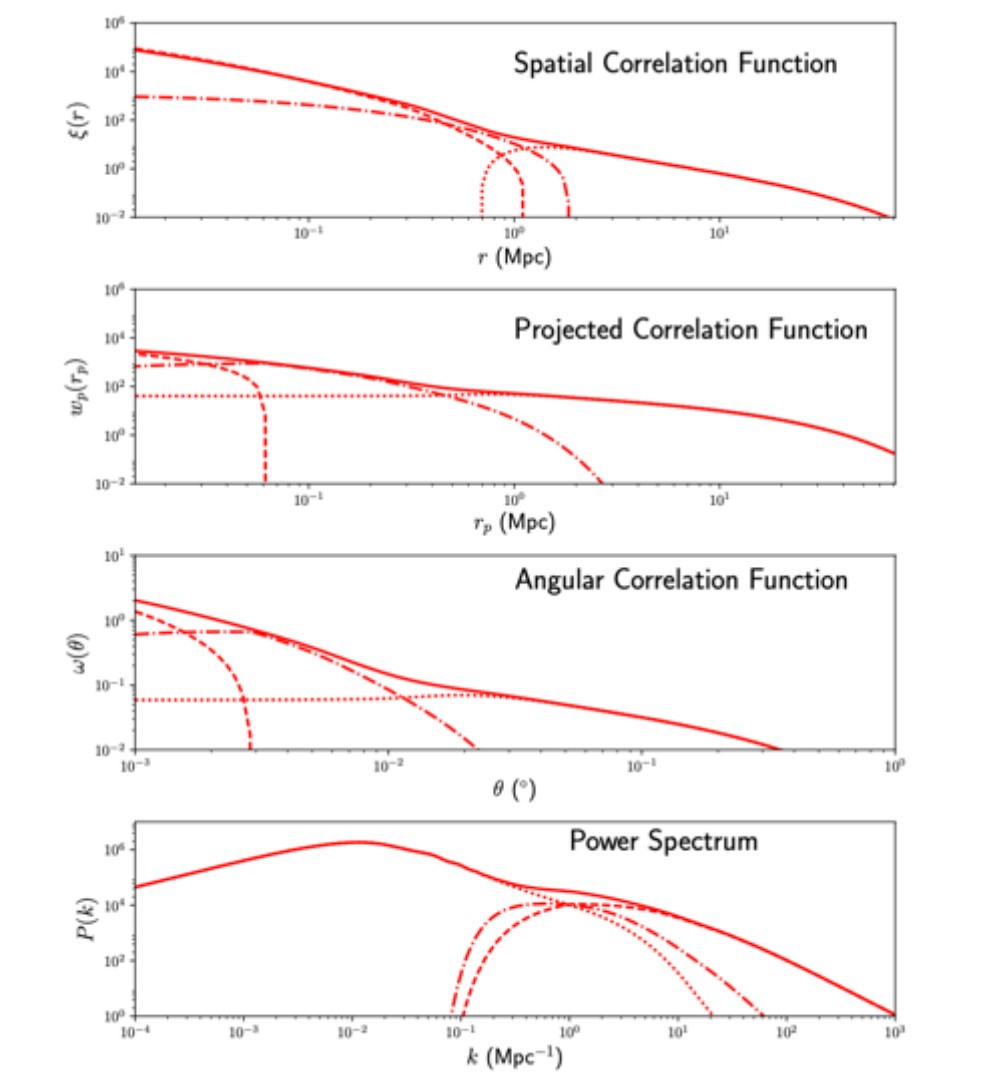
Cosmology



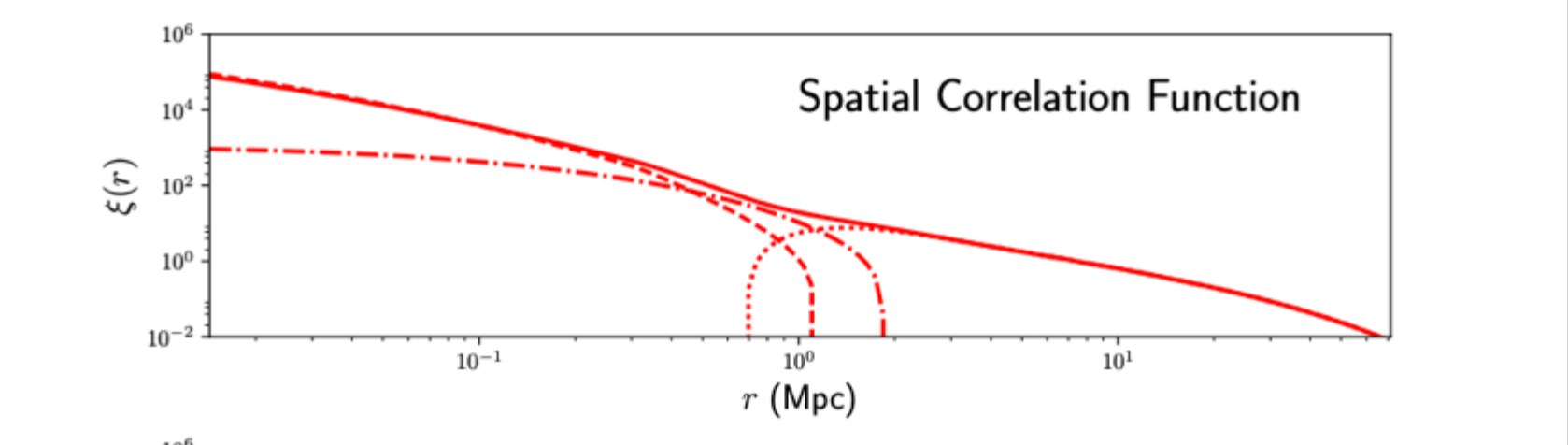
Cosmology



Galaxy Environment



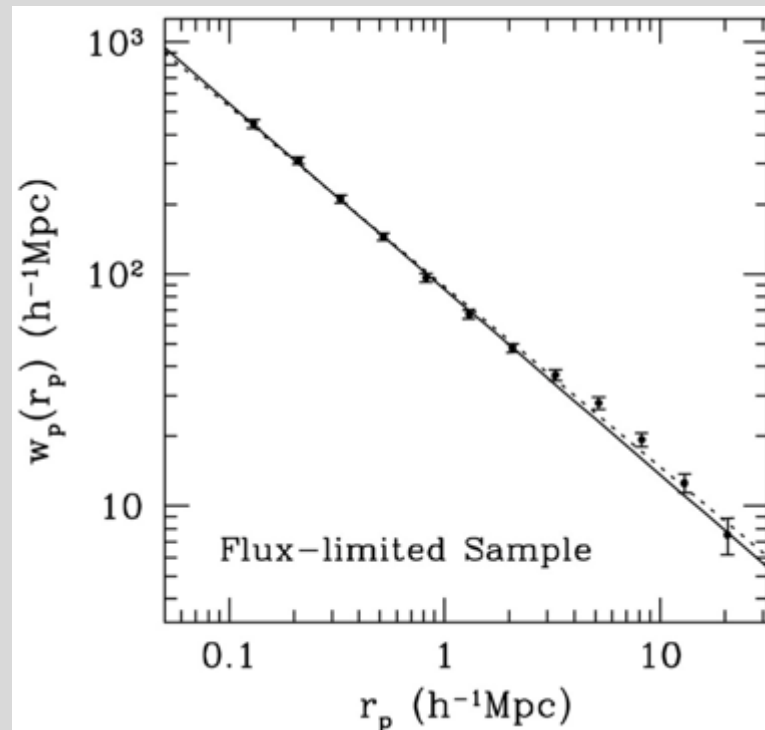
Galaxy Environment



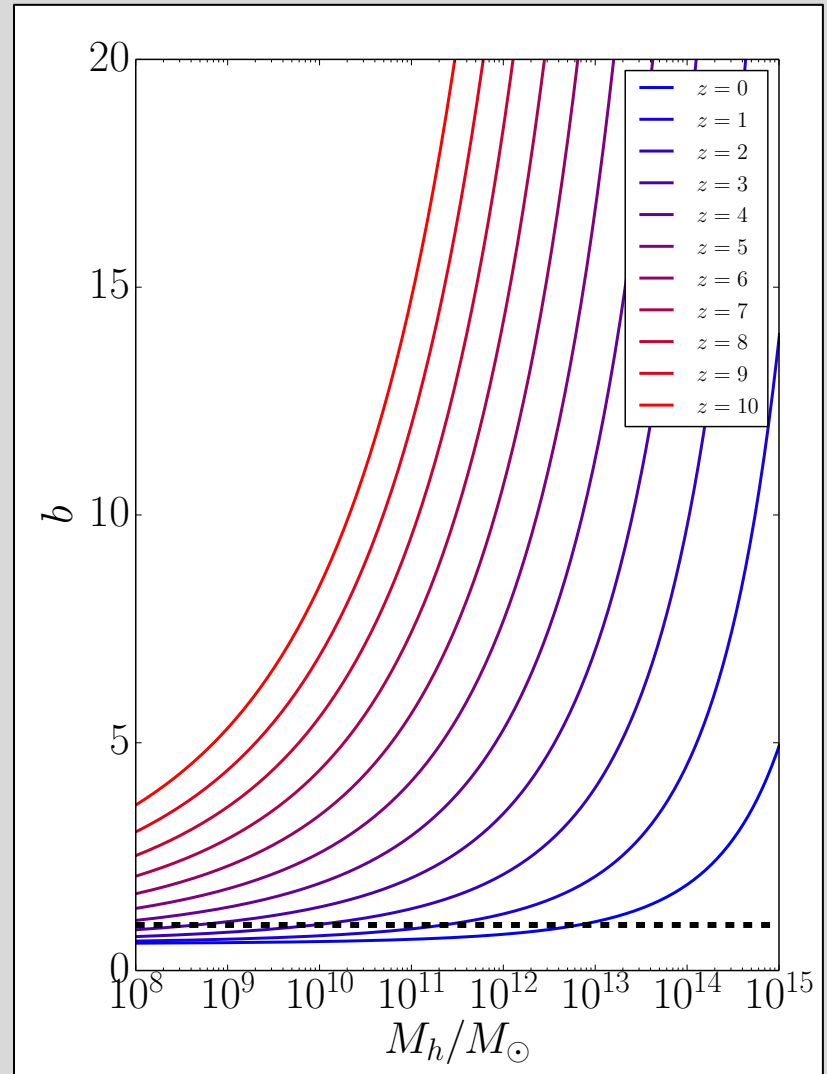
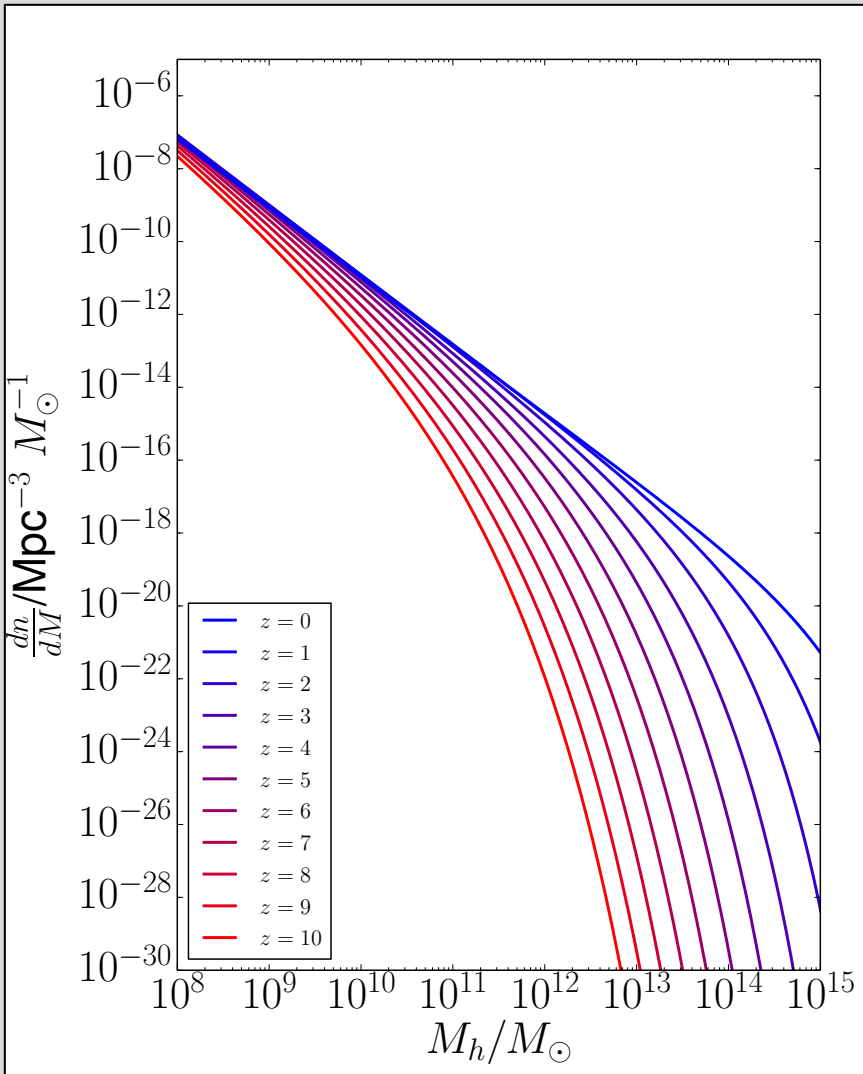
Power Law Modelling:

- Fit a power law to angular correlation function (index ~ -0.8)
- De-project to get spatial correlation function amplitude
- Compare to theoretical DM clustering amplitude
- Get a bias, and average halo mass

$$\left(\frac{\delta n}{n}\right) = b \left(\frac{\delta \rho}{\rho}\right)$$



Halo Properties Over Cosmic Time

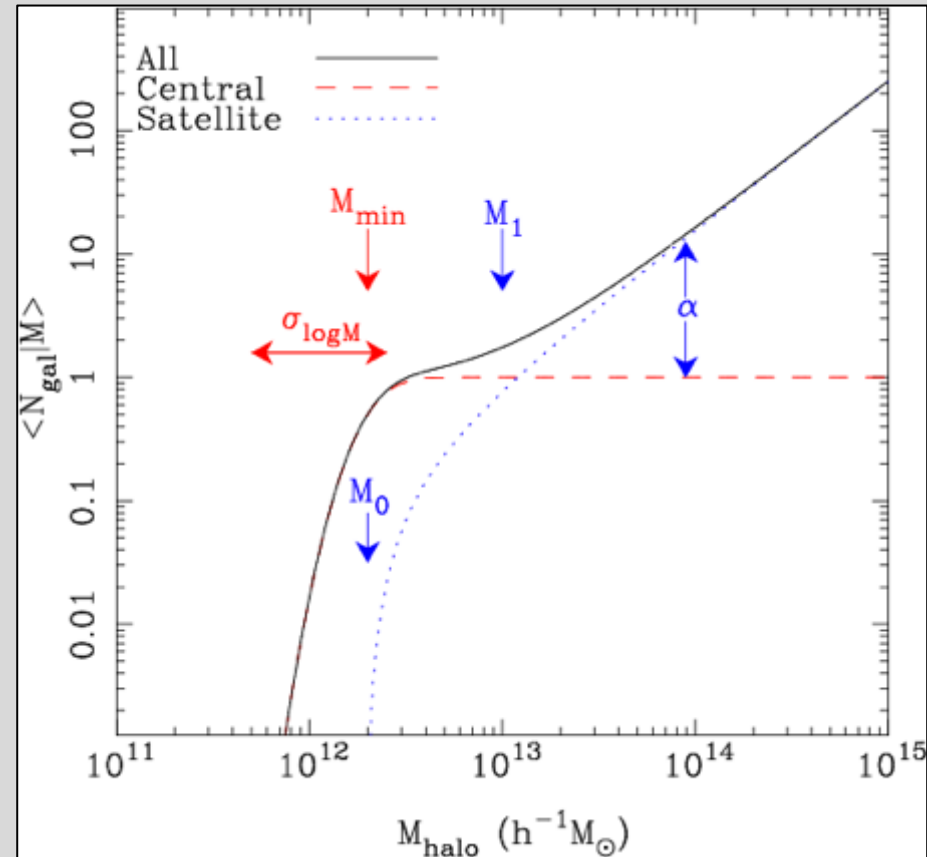


- > Measure correlation function (and other variables)
- > Generate model correlation functions from galaxy-halo relation model
- > Fit parameters

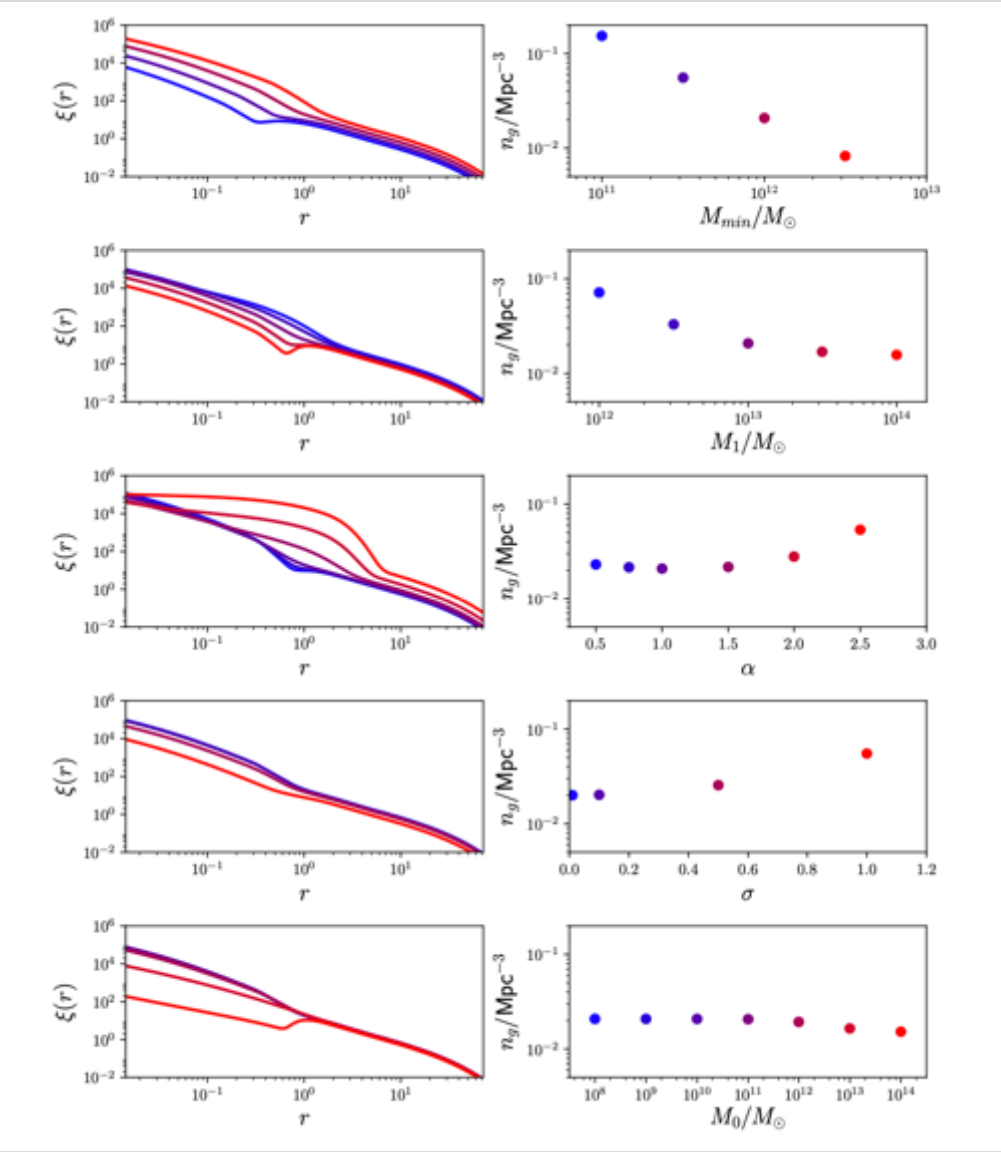
HOD Ingredients:

- (Cosmology)
- Halo mass function
- Halo bias prescription
- Dark matter power spectrum
- Halo profiles
- Occupation number
- Poisson assumption
- Central/satellite distinction
- 1-halo and 2-halo terms

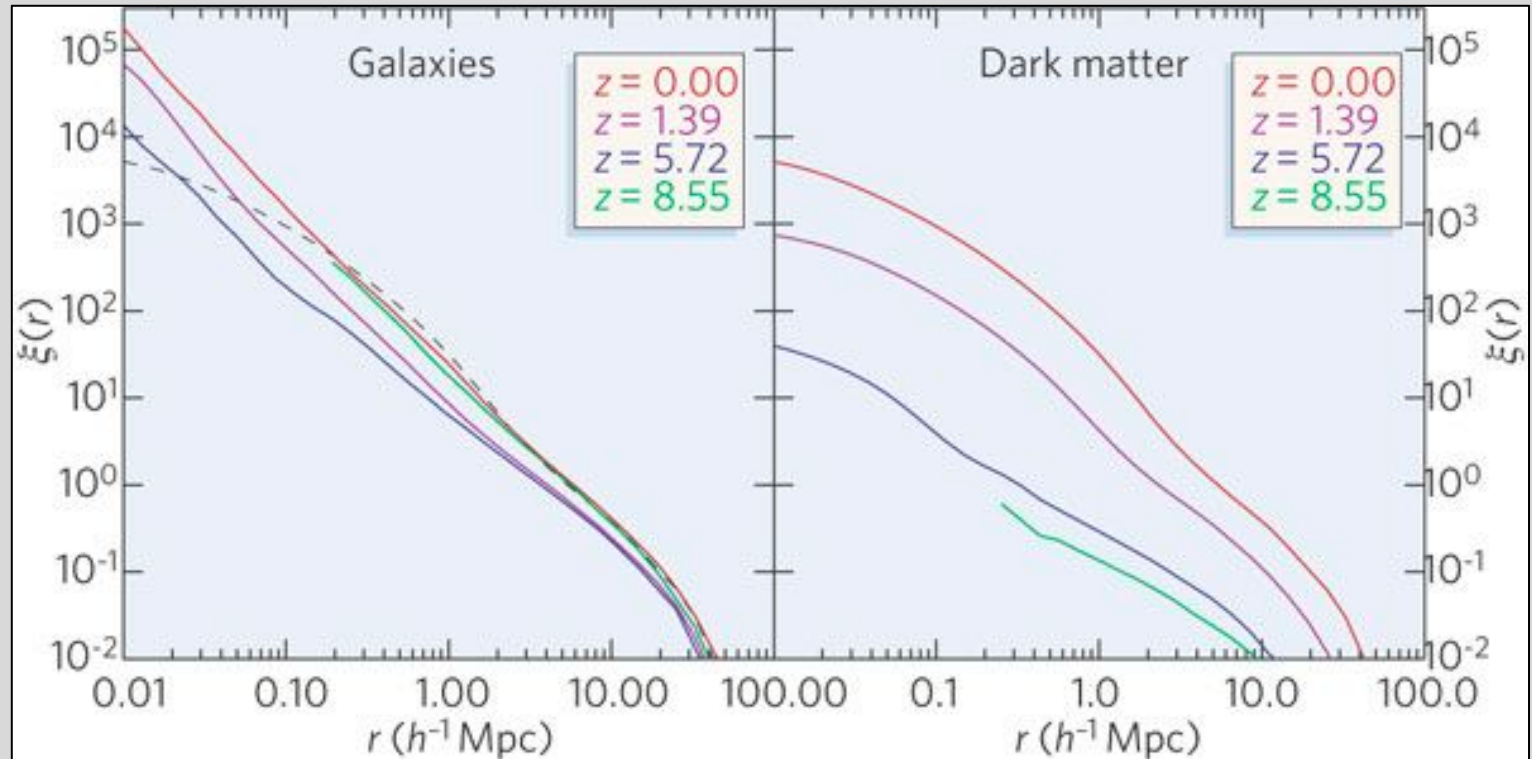
$$\chi^2 = \frac{[n_{\text{gal}}^{\text{obs}} - n_{\text{gal}}^{\text{model}}]^2}{\sigma_n^2} + \sum_i \frac{[\omega^{\text{obs}}(\theta_i) - \omega^{\text{model}}(\theta_i)]^2}{\sigma_{w_i}^2},$$



Galaxy Environment



Both the DM and the Galaxies are Evolving



Springel et al., 2006 (Millennium simulation)

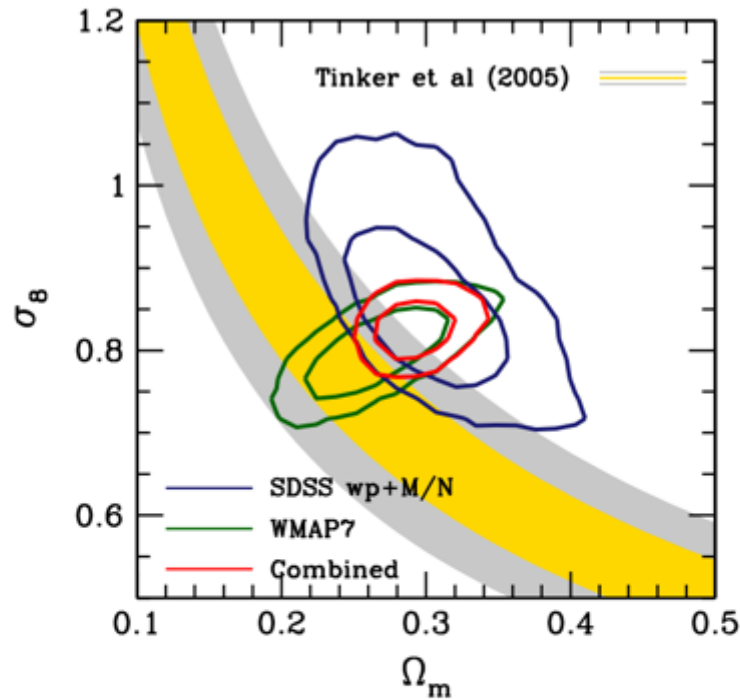
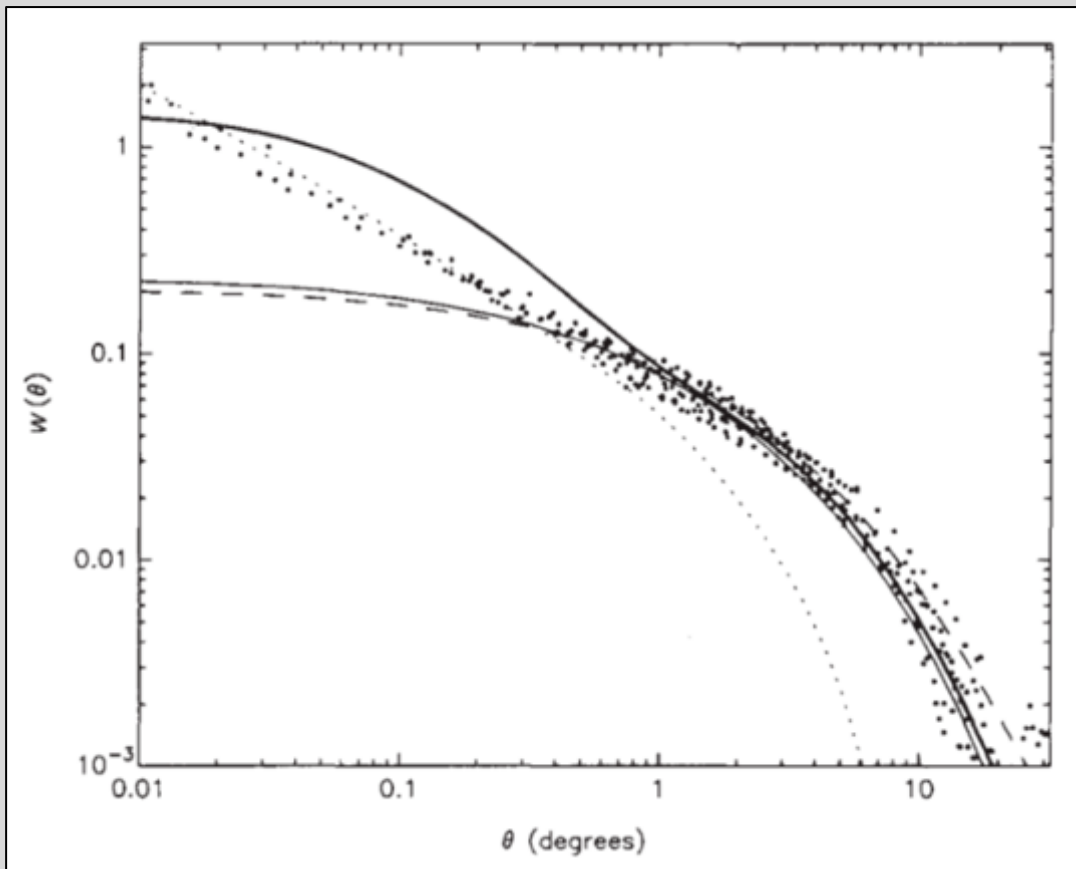


Figure 8. Constraints in the Ω_m - σ_8 plane, marginalizing over all other parameters and applying the priors listed in Table 3. The blue contours show 68% and 95% constraints from the M/N results. The yellow and gray shaded region indicates the 1σ and 2σ constraints, respectively, from Tinker et al. (2005). The green contour shows the constraints from WMAP7 (CMB alone, assuming a flat Λ CDM model; Komatsu et al. 2011). The red contours show the combined constraints from M/N and WMAP7.

(A color version of this figure is available in the online journal.)

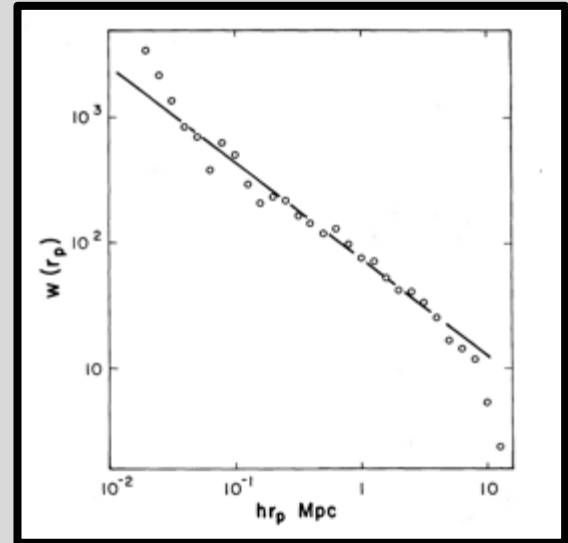
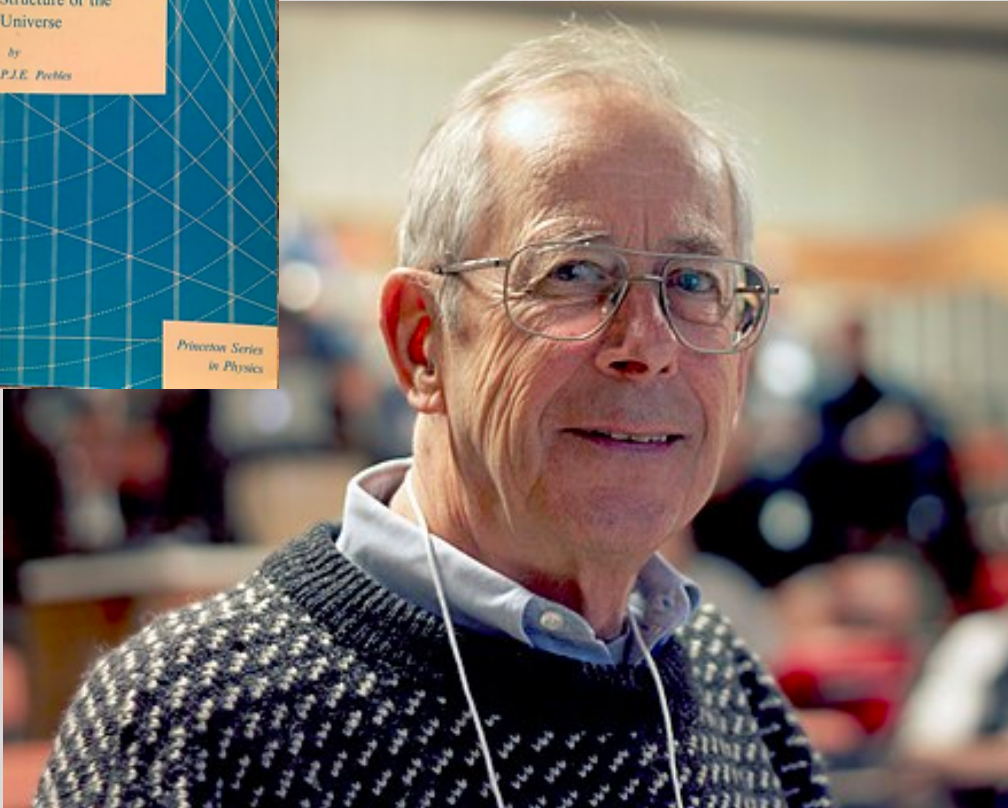
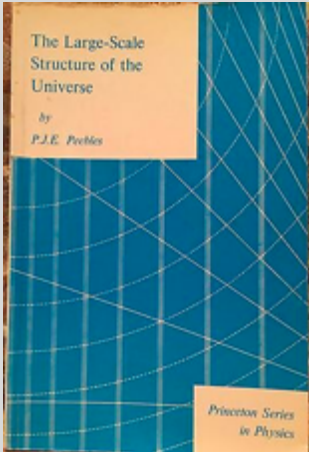
Historical Notes

Galaxy clustering in the early 1990's – an early hint of dark energy?
(SNe evidence comes out in 1998/1999, Efstathiou+1990 find suggestion of $\Omega_\Lambda \approx 0.8...$)



Historical Notes

2019 Nobel Prize in Physics goes to Jim Peebles for work on the large scale structure of the Universe! (and exoplanets)



Davis and Peebles 1982
(2400 galaxies!)

Future?

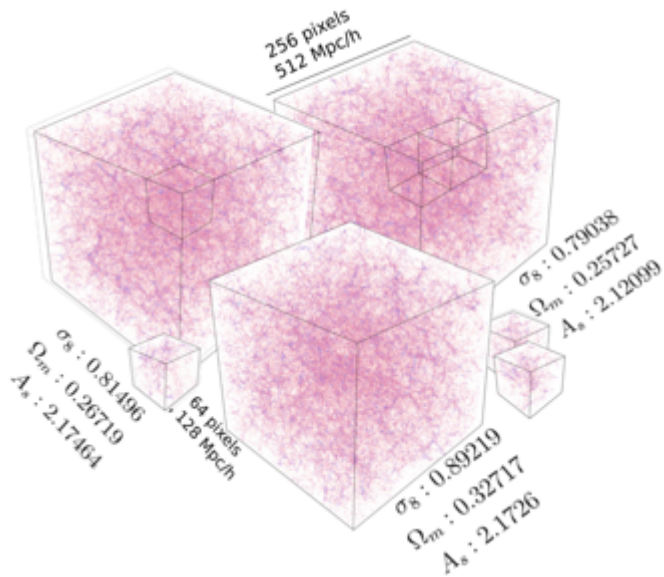


Figure 1. Dark matter distribution in three cubes produced using different sets of parameters. Each cube is divided into small sub-cubes for training and prediction. Note that although cubes in this figure are produced using very different cosmological parameters in our constrained sampled set, the effect is not visually discernible.

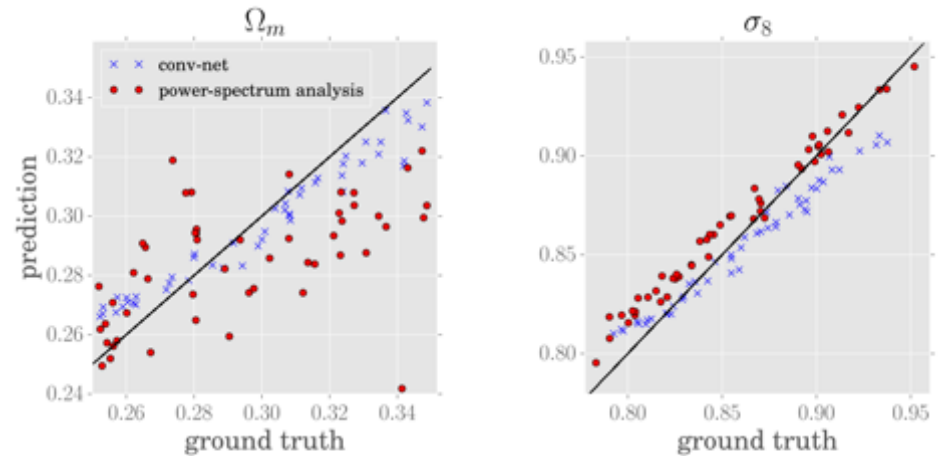


Figure 2. Prediction and ground truth of Ω_m and σ_8 using 3D conv-net and analysis of the power-spectrum on 50 test cube instances.